

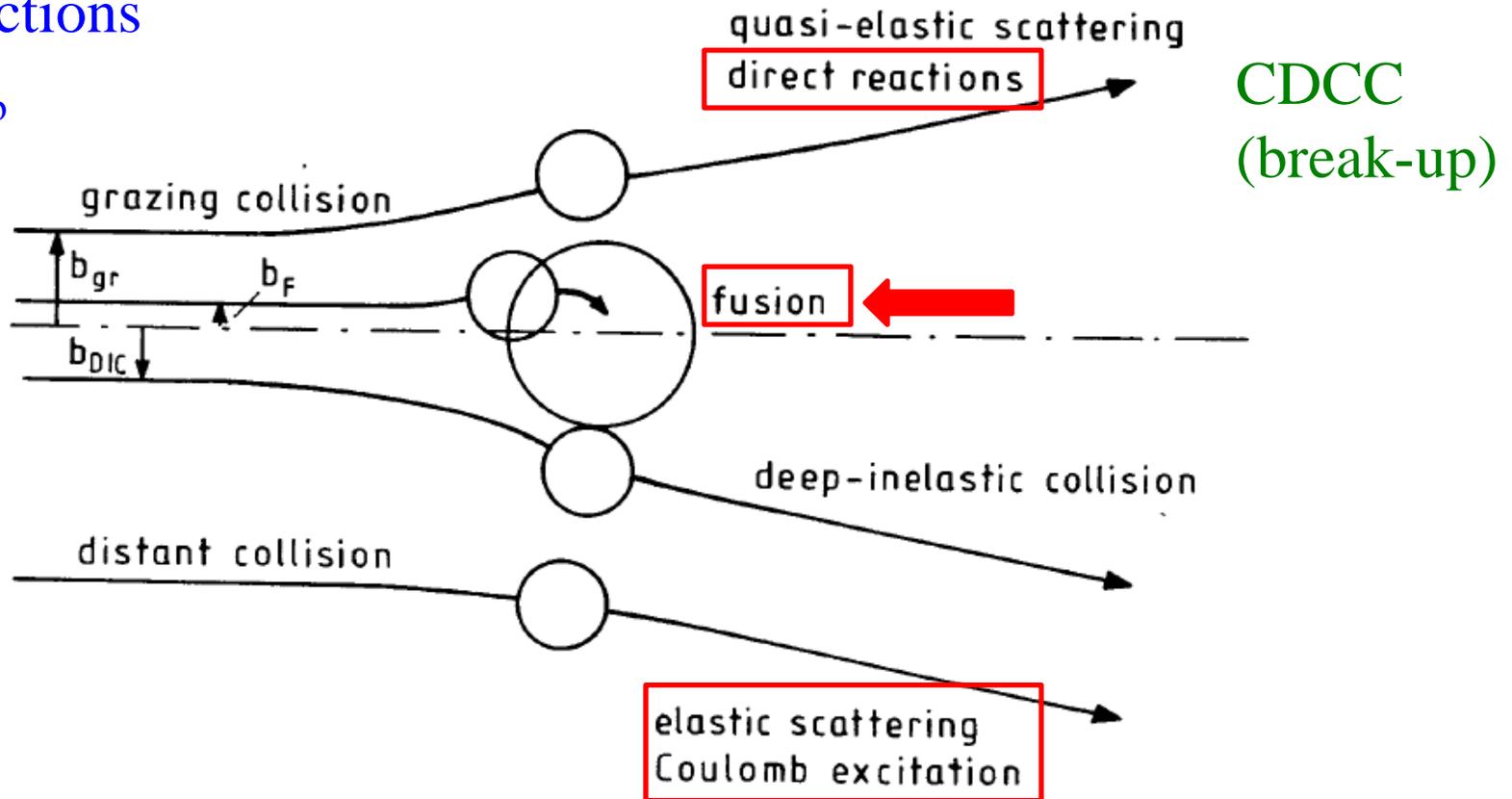
Reactions with heavy nuclei



Kouichi Hagino

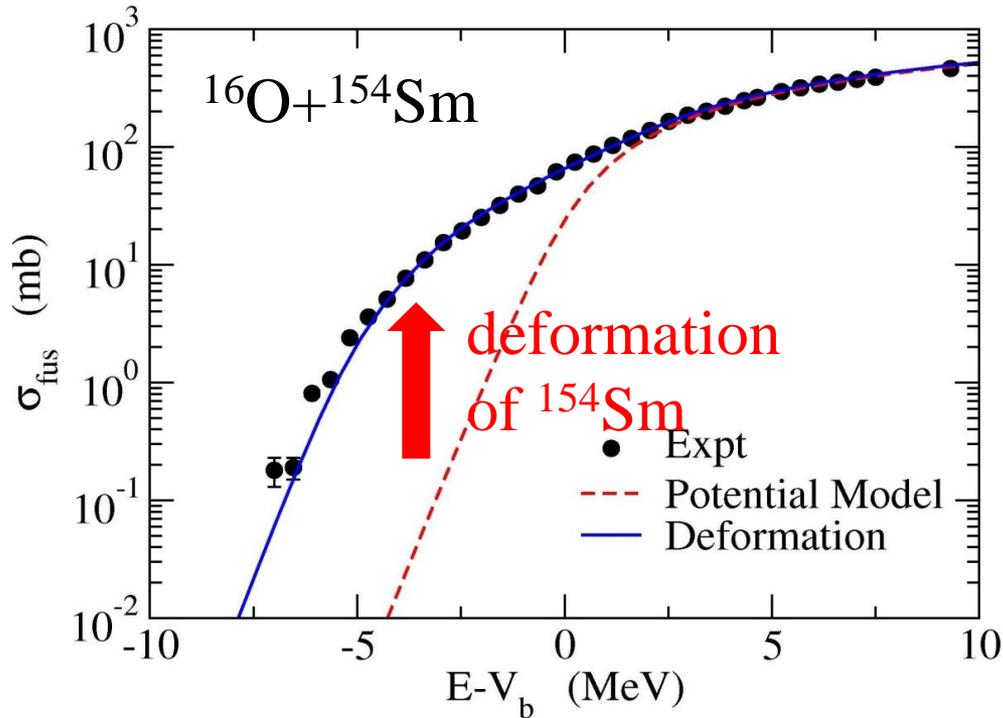
Tohoku University, Sendai, Japan

H.I. Reactions
at $E > V_b$



“Theory of Nuclear Reactions” Frobrich and Lipperheide

◆ H.I. Sub-barrier fusion reactions ($Z_P * Z_T < 1600$)



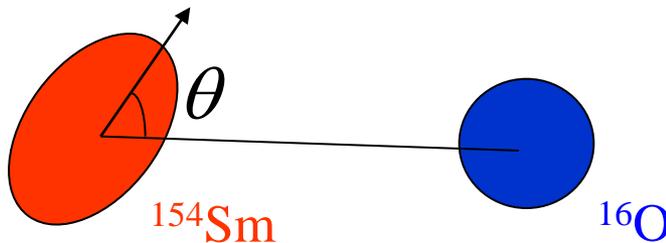
collective excitations during fusion



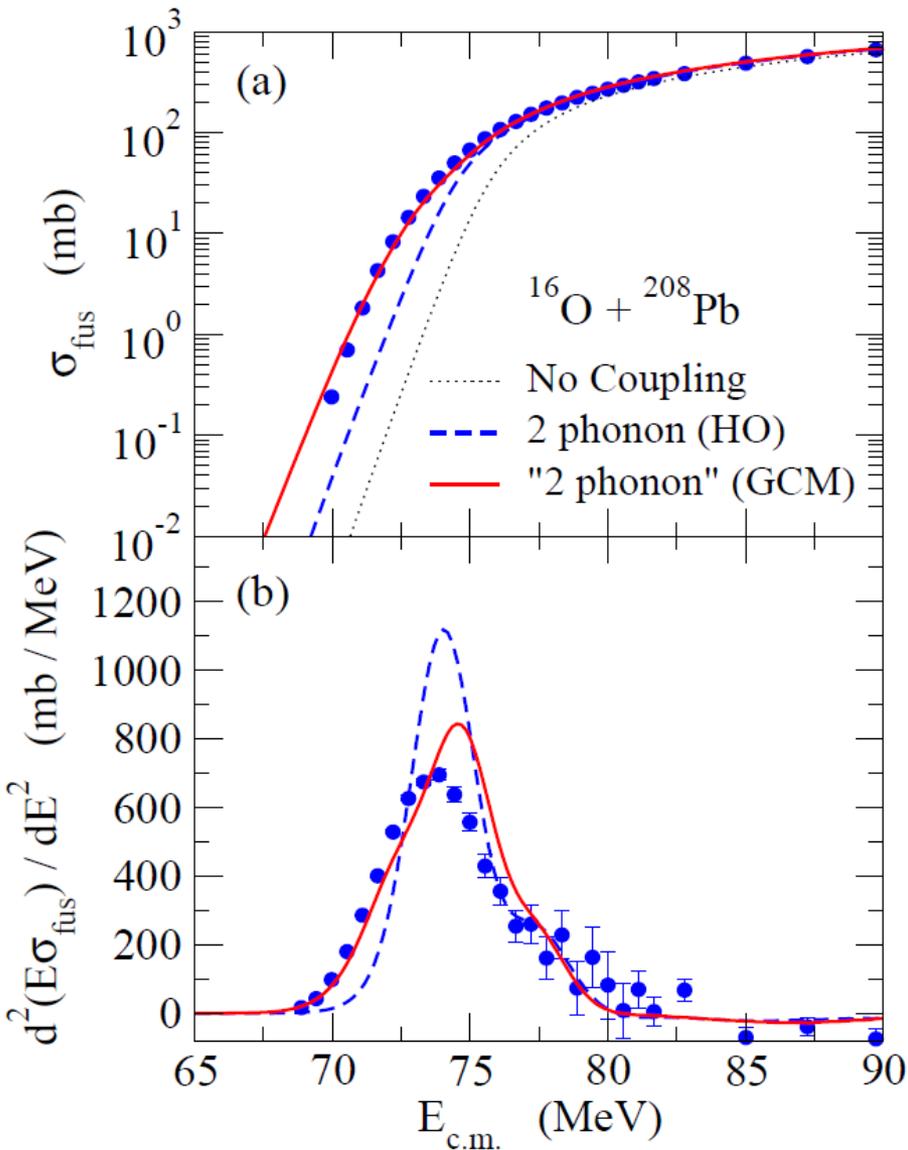
coupled-channels method

- ✓ excitation energies
- ✓ transition strengths
- ✓ multi-phonon excitations or g.s. rotational band

$$\sigma_{\text{fus}}(E) = \int_0^1 d(\cos \theta) \sigma_{\text{fus}}(E; \theta)$$

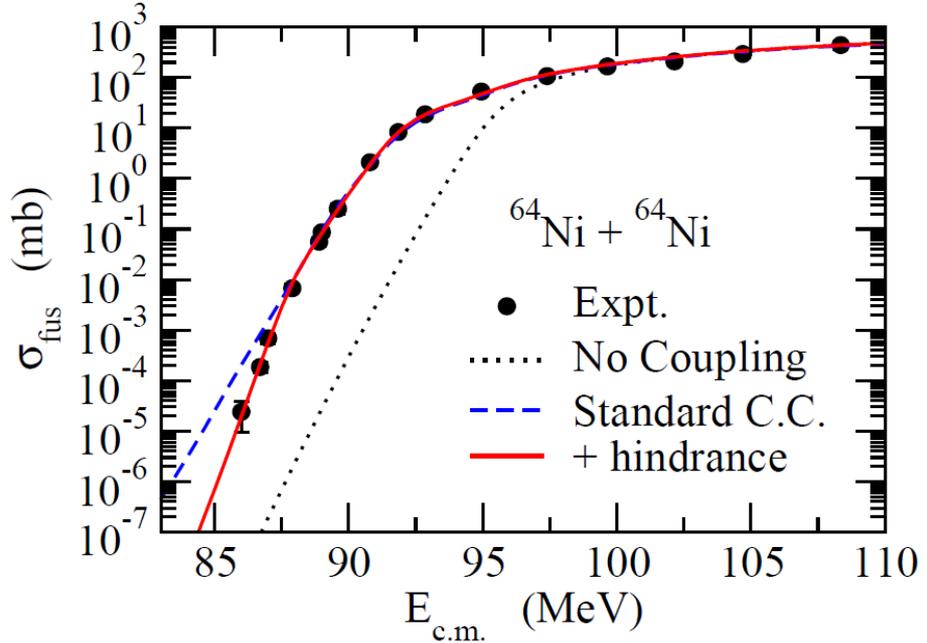
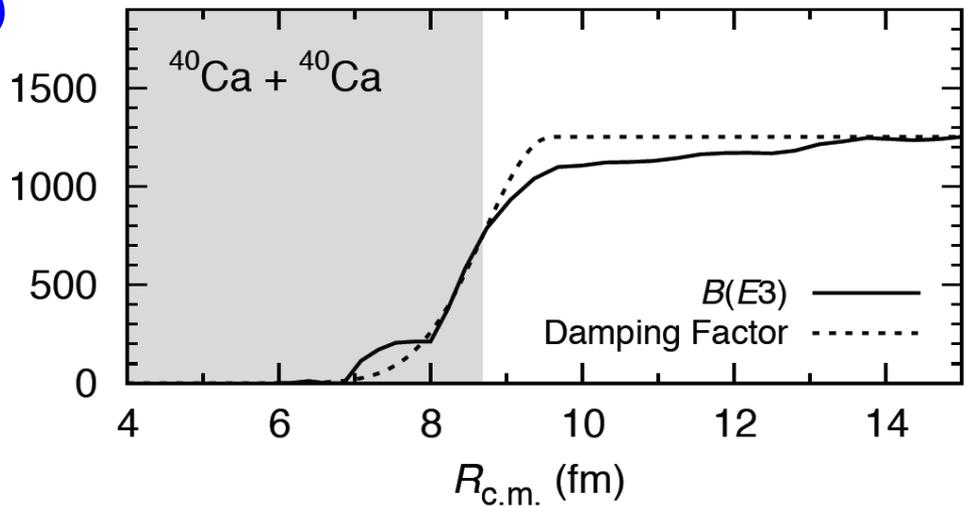


✓ C.C. with a state-of-the-art nuclear structure calculation (beyond-MF)



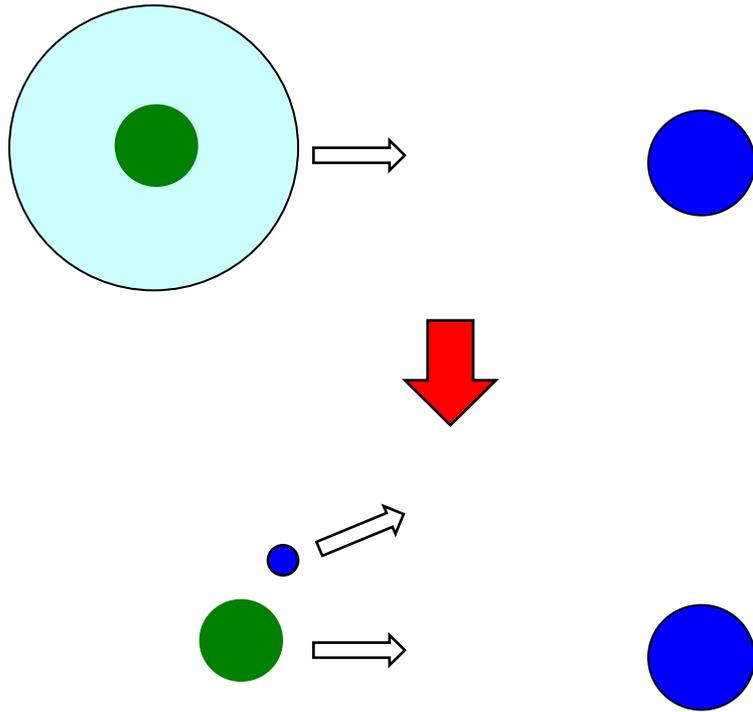
J.M. Yao and K.H. (2016)

✓ C.C. with RPA



T. Ichikawa and K. Matsuyanagi
PRC88('13) 011602(R)

Fusion of halo nuclei

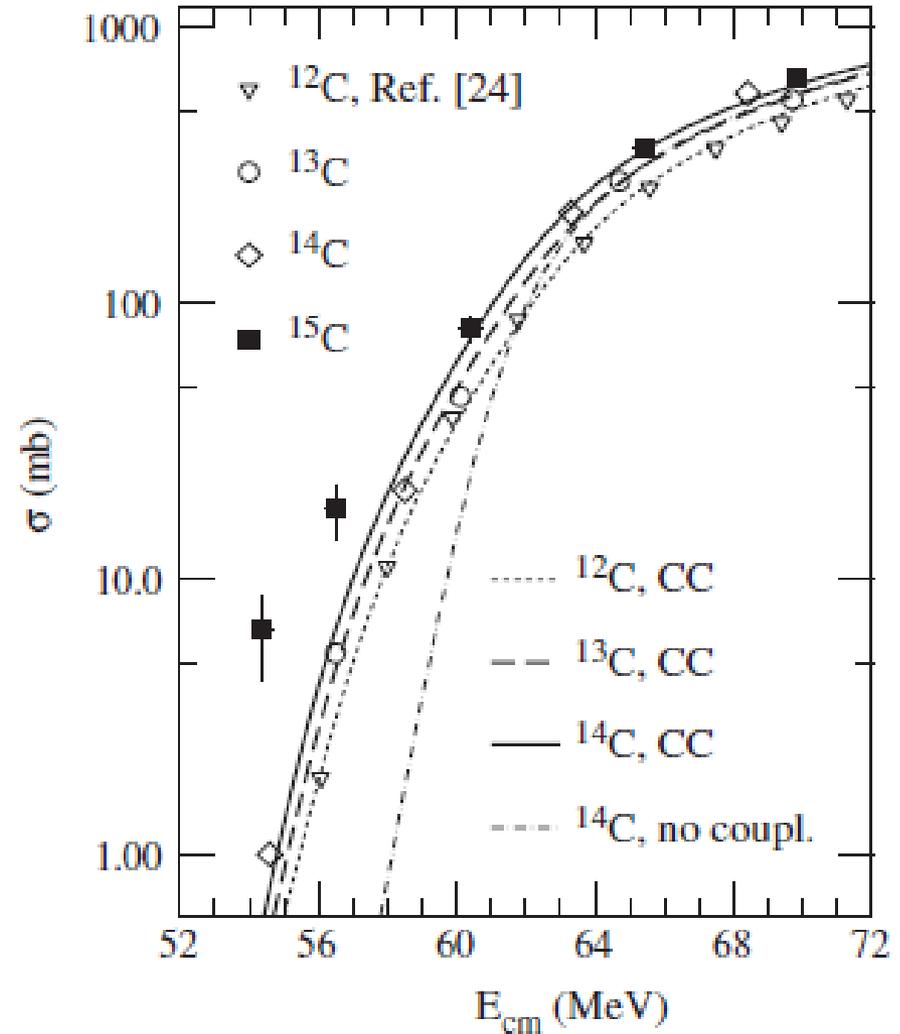


1. Lowering of potential barrier
due to a halo structure

→ enhancement

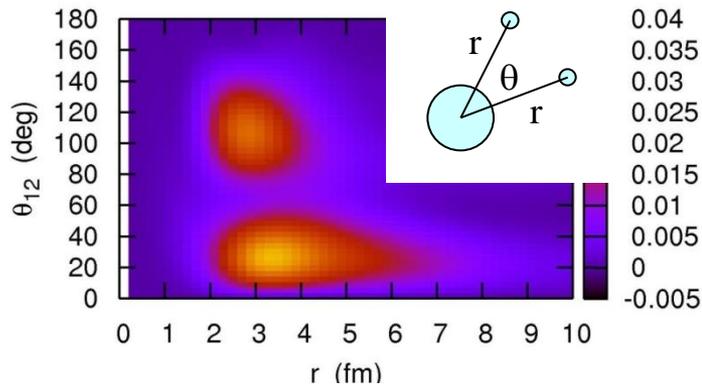
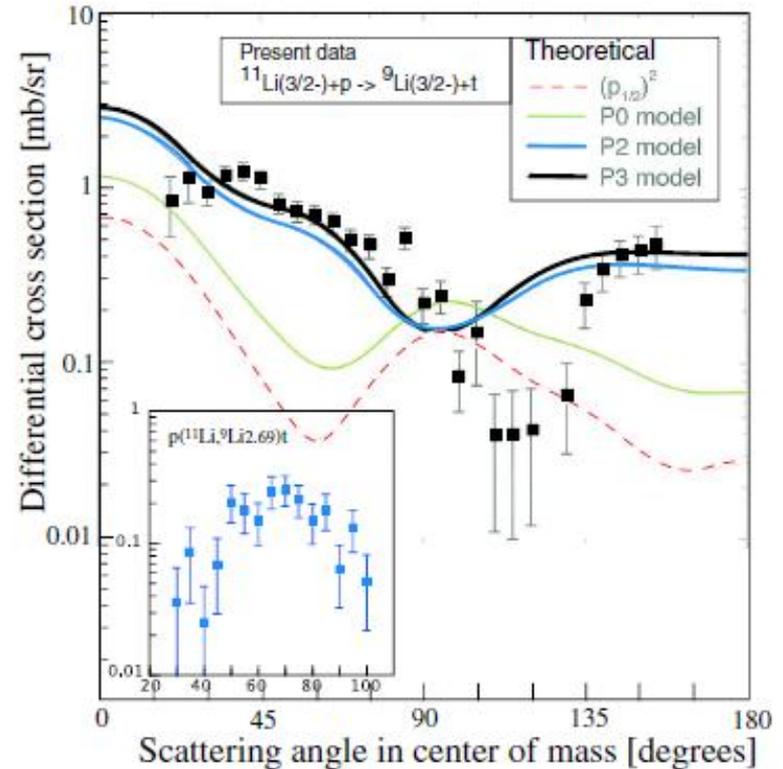
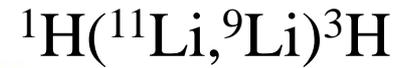
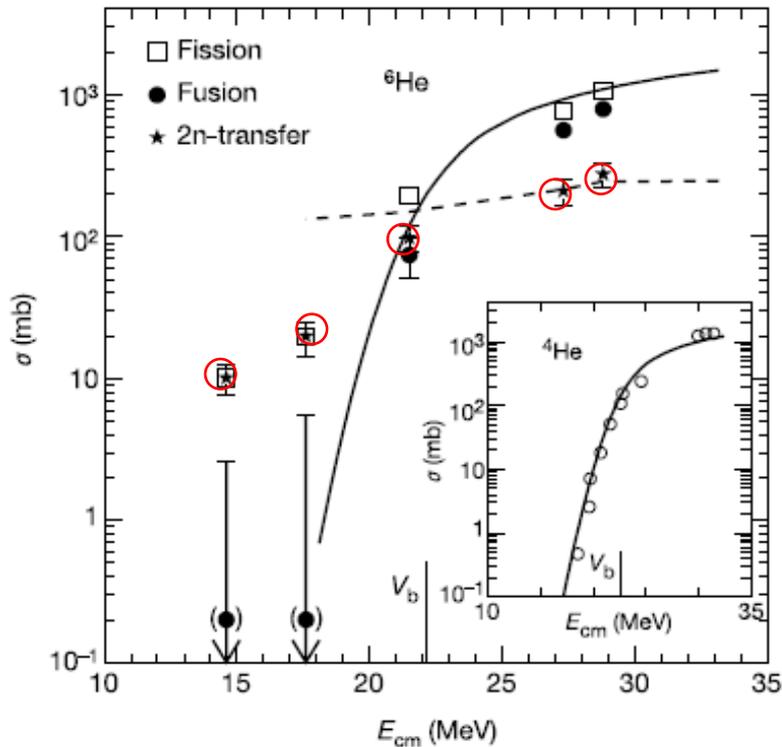
2. effect of breakup
3. effect of transfer

$^{12,13,14,15}\text{C} + ^{232}\text{Th}$



M. Alcorta et al.,
PRL106('11)172701

Two-neutron transfer reactions: pairing correlations

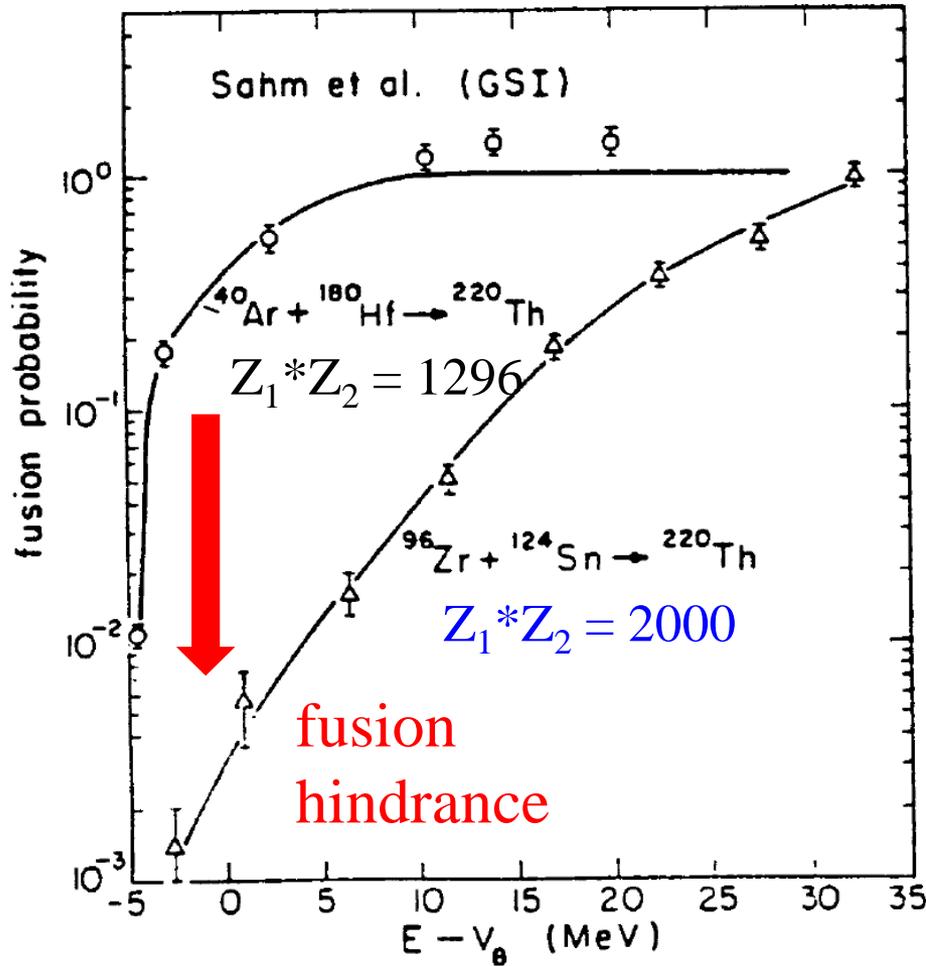


I. Tanihata et al., PRL100('08)192502

- ✓ reaction mechanism?
- ✓ role of unbound intermediate states?

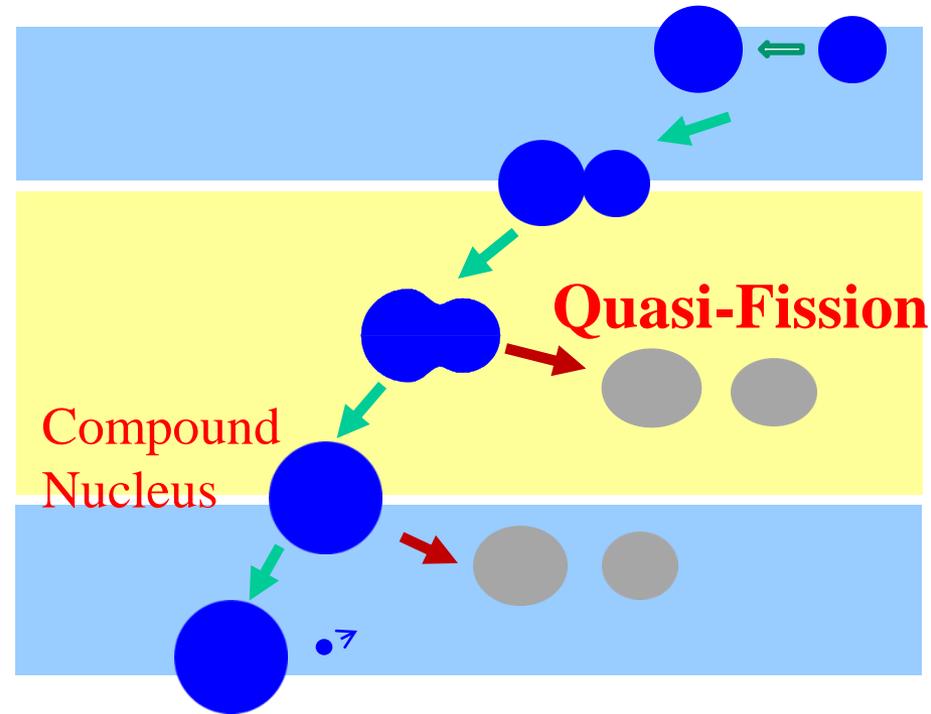
◆ H.I. Sub-barrier fusion reactions ($Z_P * Z_T > 1600 \sim 1800$)

fusion hindrance



C.-C. Sahm et al.,
 Z. Phys. A319('84)113

modern understanding

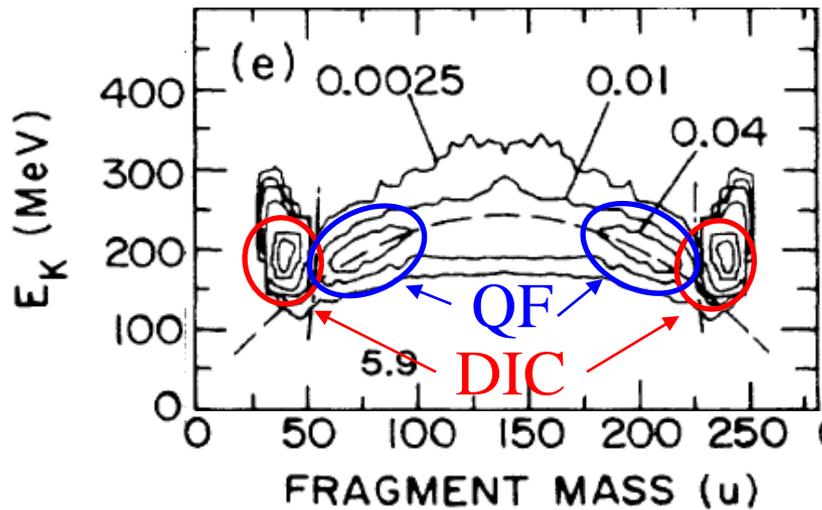


re-separation before CN
 = Quasi-Fission

closely related phenomenon: deep inelastic collision (~ 70-80's)

$^{40}\text{Ca} + ^{238}\text{U}$ ($E = 5.9 \text{ MeV/A}$)

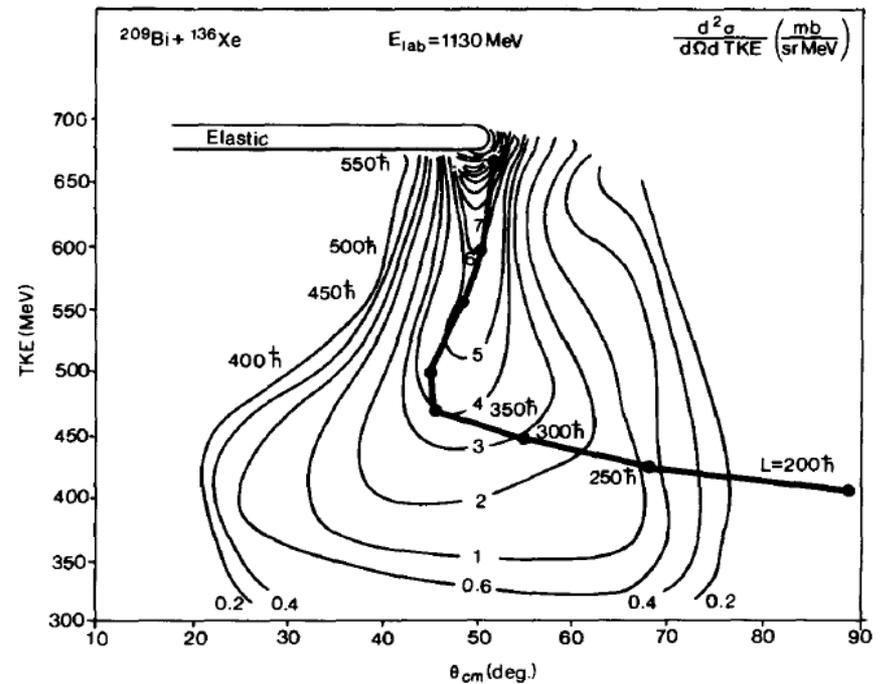
highly damped reaction



W.Q. Shen et al., PRC36('87)115

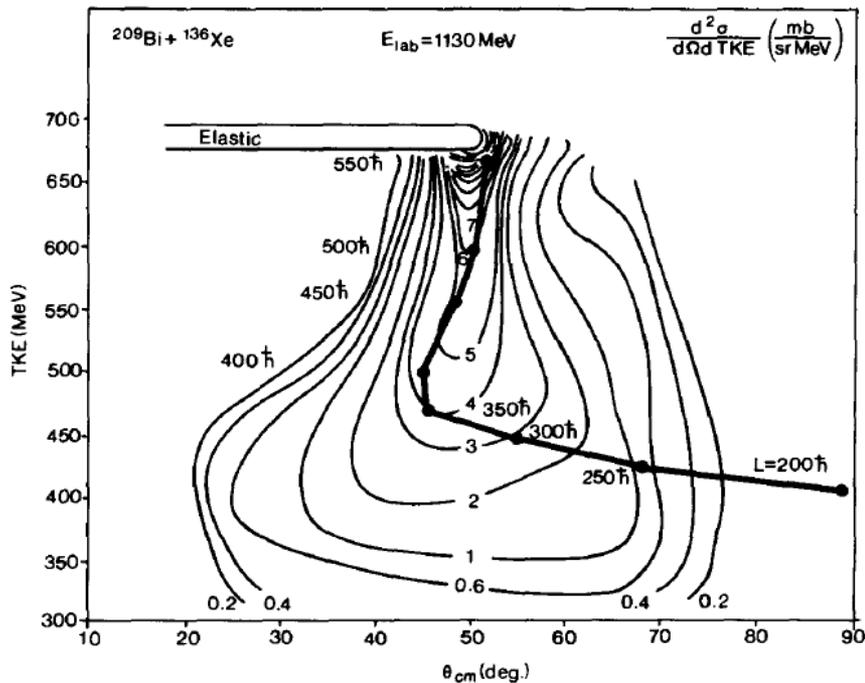
- ✓ many phenomenological models
- ✓ TDHF

a big success of TDHF:



A.K. Dhar, B.S. Nilsson,
K.T.R. Davies and S.E. Koonin,
NPA364 ('81)105

a big success of TDHF for DIC



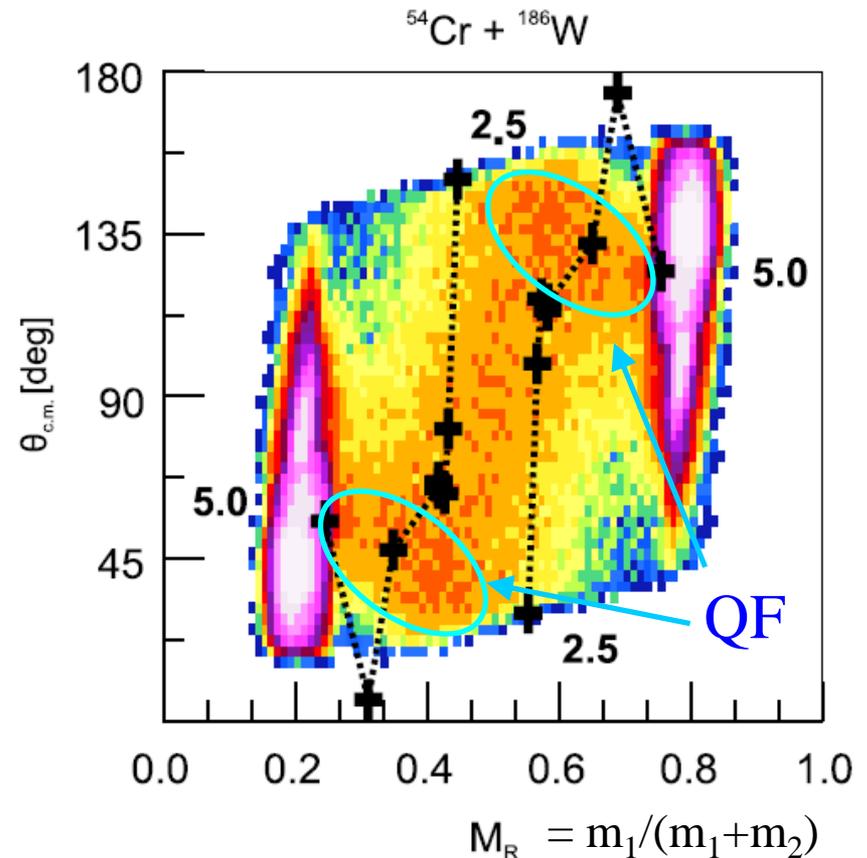
A.K. Dhar, B.S. Nilsson,
K.T.R. Davies and S.E. Koonin,
NPA364 ('81)105

➤ nuclear friction from TDHF

K. Washiyama, D. Lacroix, and
S. Ayik, PRC79('09)024609

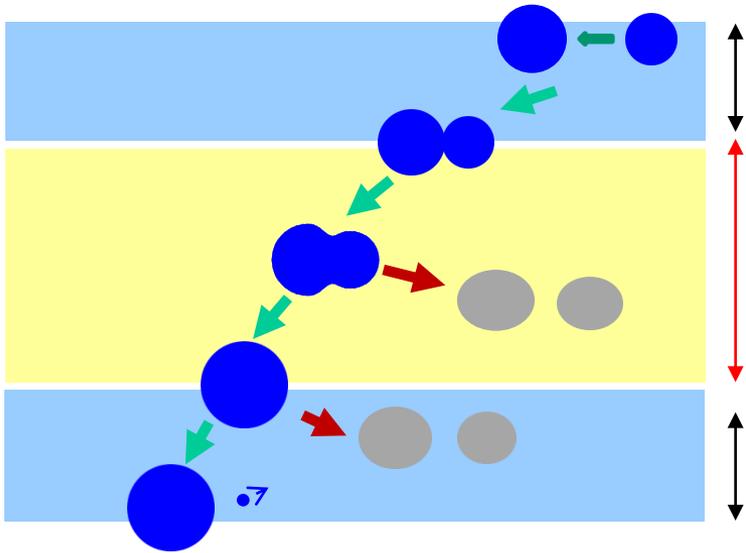
TDHF seems to work for
QF as well

mass-angle distribution



A.S. Umar and V.E. Oberacker,
NPA944('15)238
c.f. expt.: ANU group (D.J. Hinde et al.)

Super-heavy nuclei



coupled-channels method

Langevin approach

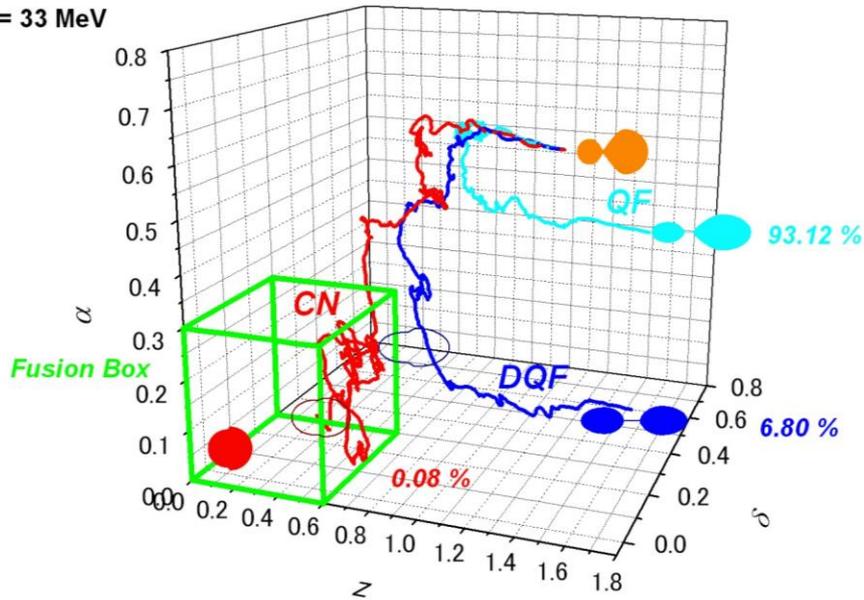
V.I. Zagrebaev and W. Greiner, NPA944('15)257

$$m \frac{d^2 q}{dt^2} = - \frac{dV(q)}{dq} - \gamma \frac{dq}{dt} + R(t)$$

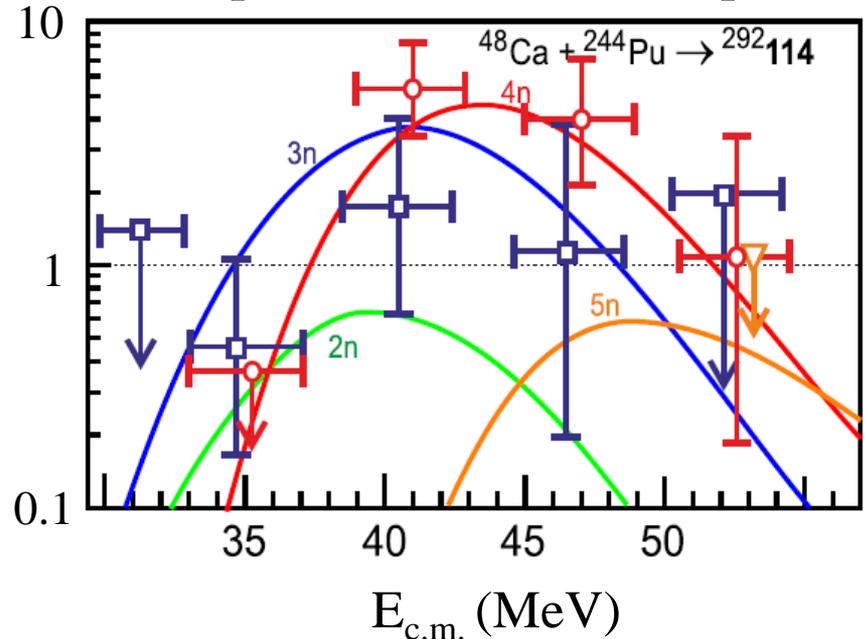
statistical model

$^{48}\text{Ca} + ^{244}\text{Pu} \rightarrow ^{292}\text{114}$

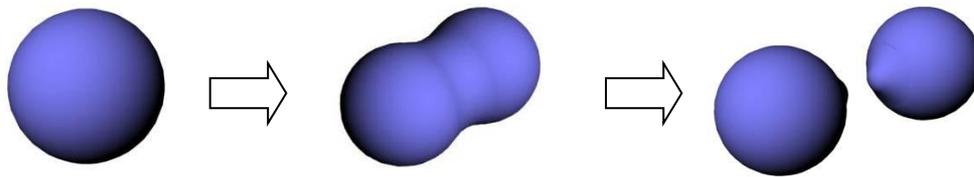
$E^* = 33 \text{ MeV}$



Evap. resid. cross section (pb)

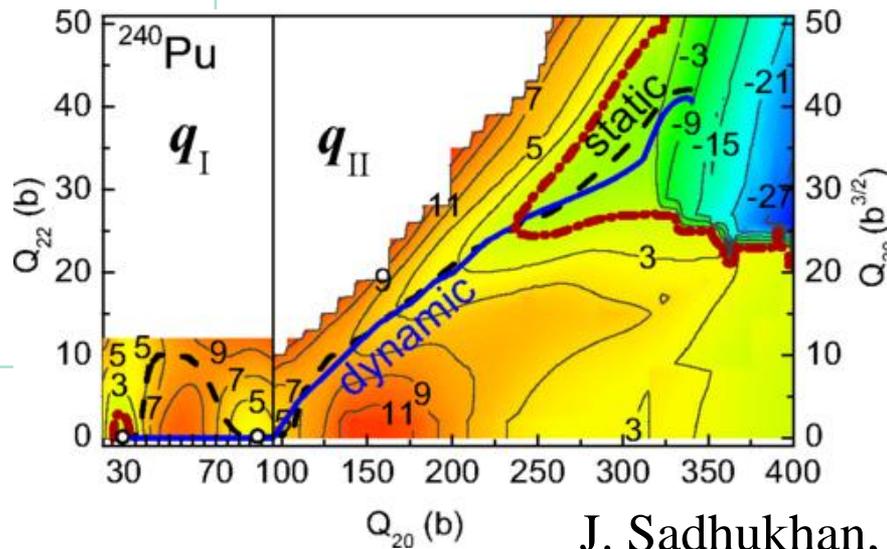


Fission



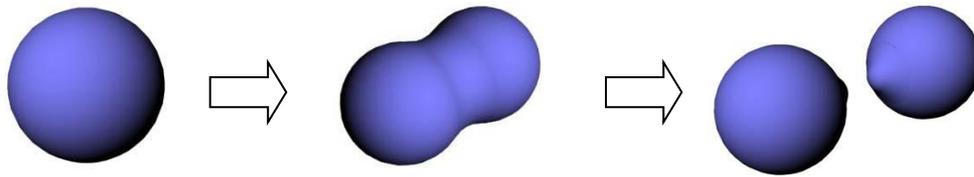
still a very challenging problem for nuclear theory

	Time-indep. approach	Time-dep. approach
Induced fission	✓ Bohr-Wheeler	✓ Langevin-type ✓ Discrete basis (Bertsch)
Spontaneous fission	✓ PES+Mass+WKB	✓ Im.-time TDHF (Negele) ✓ Time-dep. Hill-Wheeler (Goutte et al.) ✓ TDHF (after the barrier)



J. Sadhukhan, W. Nazarewicz, N. Schunck,
PRC93('16)011304(R)

Fission



still a very challenging problem for nuclear theory

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issues:

- which degrees of freedom? (time-indep. approaches)
- how to deal with many-body tunneling? (time-dep. approaches)

Summary and discussions

➤ Heavy-ion reactions around the Coulomb barrier : strong interplay between structure and reaction

- sub-barrier fusion reactions (coupled-channels effects)
- fusion of massive nuclei (nuclear friction)
- spontaneous and induced fissions
- **two-neutron transfer (pairing correlations)**

➤ From phenomenological models to more microscopic models

- C.C. with microscopic inputs
- DFT for spontaneous fission
- TDHF approach ←

➤ “Beyond mean-field” approximations

Full time-dependent GCM? $|\Psi(t)\rangle = \int dq f(q, t) |\Phi_q(t)\rangle$
→ many-body tunneling

cf. “Quantum tunneling using entangled classical trajectories”
A. Donoso and C.C. Martens, PRL87 ('01) 223202